

Problems Involving Complex Numbers, with an Emphasis on Polar Form

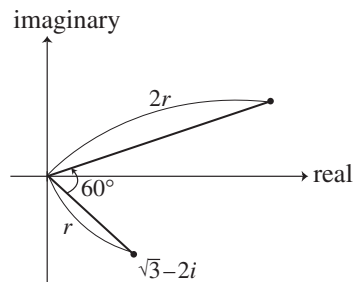
(fx-100MS/fx-115MS/fx-570MS/fx-991MS only)

Example 1

Rotate $\sqrt{3} - 2i$ 60 degrees around the origin of the complex plane, and then determine the point with a ratio of 2 with the origin as the center.

Explanation

Defining r as the distance of point (a, b) from the origin on the complex plane and θ as the angle formed with the positive part of the x -axis makes it possible to express complex number $z = a + bi$ as $z = r(\cos\theta + i\sin\theta)$. This is called polar representation of complex number z . Using polar representation for z_2 in the complex number multiplication $z_1 \times z_2$ gives us $z_2 = r_2(\cos\theta_2 + i\sin\theta_2)$. Now we can rotate z_1 θ_2° around the origin of the complex plane, giving us a value with a ratio of r_2 with the origin as the center.



Operation

1. Select the CMPLX Mode.

MODE 2

2. Specify the angle unit .

MODE MODE MODE MODE 1 (Deg)

3. Input the polar form of the complex number, with $r = 2$, and $\theta = 60$. The values you input are automatically converted to rectangular form on the display, but you can also display them in polar form.

2 SHIFT ∠ 60 =

SHIFT Re↔Im

CMPLX 0 R↔I
2∠60
1

CMPLX 0 R↔I
2∠60
1.732050808i

4. Multiply by $\sqrt{3} - 2i$.

\times ($\sqrt{}$ 3 $-$ 2 i) $=$

SHIFT $\text{Re} \leftrightarrow \text{Im}$

CMPLX $\text{AnsX}(\sqrt{3}-2i)$ $\text{Re} \leftrightarrow \text{Im}$
5.196152423

CMPLX $\text{AnsX}(\sqrt{3}-2i)$ $\text{Re} \leftrightarrow \text{Im}$
 i

The above obtains the complex number $5.196152423 + i$.