

* Deflection of Beams

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① Simply Supported Beam

F: Force

L: Beam Length

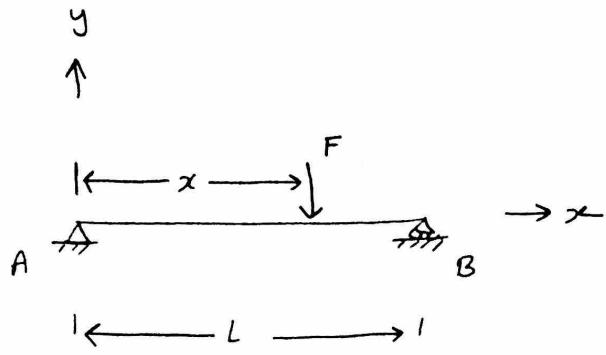
- Reactions at A and B

- Deflection $y(x)$

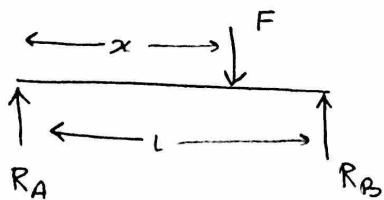
To find reactions

$$\Rightarrow \sum M_A = 0 \text{ and } \sum M_B = 0$$

$$\Rightarrow \begin{cases} R_A = F\left(1 - \frac{x}{L}\right) \\ R_B = F \frac{x}{L} \end{cases} \text{ Eq(a)}$$



Free-body diagram



Deflection

$$\frac{d^2y}{dx^2} = \frac{M}{EI} \Rightarrow y(x) = \frac{1}{EI} \left[\int_0^x \left(\int_0^x M(x) dx \right) dx + C_1 x + C_2 \right]$$

C_1 and $C_2 \Rightarrow$ Constants \Rightarrow from Boundary Conditions

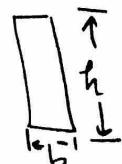
$$y(x) = \frac{FL^3}{48EI} \left(3 \frac{x}{L} - 4 \frac{x^3}{L^3} \right) \quad 0 \leq x \leq L/2$$

At center $x = L/2$

$$y(L/2) = \frac{FL^3}{48EI} \quad \text{Eq(b)} \quad , \quad E: \text{Elastic modulus}$$

I: moment of Inertia

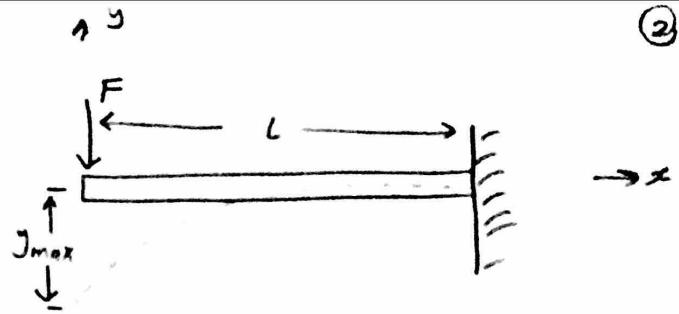
$$I = \frac{1}{12} b h^3$$



② Cantilever Beam

$x=0$

$$y_{max} = \frac{FL^3}{3EI} - Eq(c)$$



$$y(x) = \frac{F}{6EI} (-x^3 + 3L^2x - 2L^3)$$

* What will we do in the Lab?

1- Simply Supported beam

- Apply Force (F)
- Change distance x
- measure reactions at A and B
and compare to theory Eq(a)
⇒ Table 1
- measure deflections
and compare to theory Eq(b)
⇒ Table 2

2- Cantilever Beam

- Apply Force (F)
- Change Beam Length (L)
- measure Deflection and compare
to theory Eq(c)
⇒ Table 3

Distance x from support A (mm)	Experimental		Theoretical		Percentage Error (%)	
	Reaction force A (N)	Reaction force B (N)	Reaction force A (N)	Reaction force B (N)	Reaction force A	Reaction force B
100						
200						
300						
400						
500 (Center)						

Table 1: Part 1, Reaction forces.

Distance x from support A (mm)	Deflection W (Experimental) (mm)	Deflection W (Theoretical) (mm)	Percentage Error (%)
100			
200			
300			
400			
500 (Center)			

Table 2: Part 2, simply supported beam deflection.

Length L from clamp (mm)	Deflection W (Experimental) (mm)	Deflection W (Theoretical) (mm)	Percentage Error (%)
200			
300			
400			

Table 3: Part 3, cantilever beam deflection.