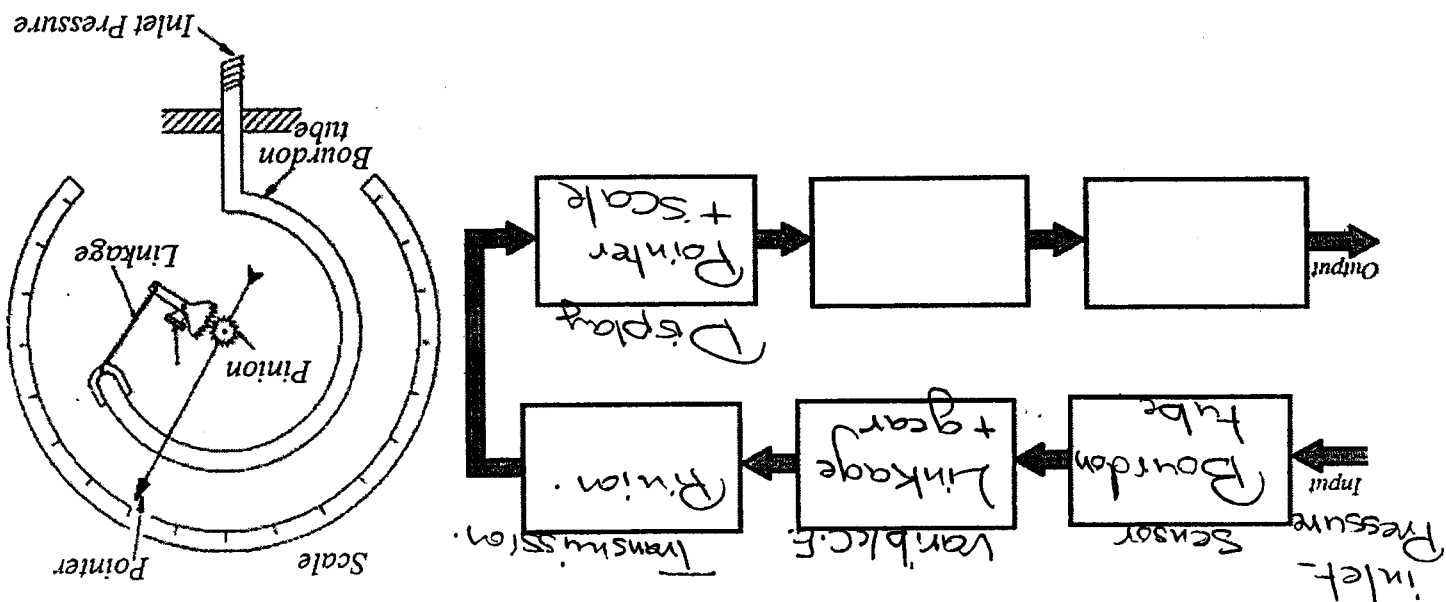


Problem 2 (3 Points)

For the shown Bourdon Tube Pressure Gage, Identify the main measuring system elements as well as the measured and output variables. (Note: there might be some extra boxes in the diagram below)



Problem 3 (4 Points)

For the second order measuring system governed by the equation:

$$2q_1 = 2q_0 + 0.12 \frac{dq_0}{dt} + 0.005 \frac{d^2q_0}{dt^2}$$

Find the following:

a. Natural Frequency

$$\left(\frac{q_0}{q_0}\right) = \omega^2 \Rightarrow \omega = \sqrt{\frac{1}{0.005}} = 20$$

b. Damping Ratio (what is the system condition)

$$\zeta = \left(\frac{q_0}{q_0}\right) \frac{1}{2} = \left(\frac{0.12}{2}\right) \frac{1}{20} = 0.5 \text{ under damped}$$

c. Steady State Output value if the input value was (7 V)

$$K = \frac{1}{2} = 1 \Rightarrow q_0 = K q_c \Rightarrow q_0 = 7V$$

d. System output after (125 msec) for the same input in (c)

$$q_0 = 7 \left(1 - e^{-(0.6) \times 20 (125 \times 10^{-3})} \sin \left(\sqrt{1 - 0.6^2} \times 20 (125 \times 10^{-3}) + \phi \right) \right)$$

$$\phi = \sin^{-1} \sqrt{1 - 0.6^2} = 0.927$$

$$q_0 = 7 (1 - e^{-1.5} \sin(2.927)) = (1 - 0.0475) 7$$

$$= 6.667 V$$