

EXAMPLE 1-2

A solid circular rod of diameter d undergoes a bending moment $M = 100 \text{ N} \cdot \text{m}$ inducing a stress $\sigma = 16M/(\pi d^3)$. Using a material strength of 170 MPa and a *design factor* of 2.5, determine the minimum diameter of the rod. Using Table A-17, select a preferred fractional diameter and determine the resulting *factor of safety*.

Solution From Eq. (1-3), $\sigma = S/n_d$, then

$$\sigma = \frac{16M}{\pi d^3} = \frac{S}{n_d}$$

Solving for d yields

Answer
$$d = \left(\frac{16Mn_d}{S\pi} \right)^{1/3} = \left(\frac{16(100)2.5}{170(10)^6 \pi} \right)^{1/3} = 0.0196 \text{ m} = 19.6 \text{ mm}$$

From Table A-17, the next higher preferred size is ~~20~~ mm. Thus, when n_d is replaced with n in the equation developed above, the factor of safety n is

Answer
$$n = \frac{\pi S d^3}{16M} = \frac{\pi(170)(10^6)(0.020)^3}{16(100)} = 2.67$$